



Formulae On Integrals

Indefinite Integrals of some important functions

The indefinite integral, also known as the **anti-derivative**, represents a family of functions whose derivative is the given function. It includes an arbitrary constant C , since differentiation of a constant is zero. The notation for an indefinite integral is:

$$\int f(x) dx = F(x) + C$$

Where, $F(x)$ is the antiderivative of $f(x)$.

| | |
|---|--|
| 1. $\int dx = x + C$ | 2. $\int a dx = ax + C$ |
| 3. $\int x^n dx = \frac{x^{n+1}}{n+1} + C$ | 4. $\int a^x dx = \frac{a^x}{\log a} + C$ |
| 5. $\int \frac{1}{x} dx = \log x + C$ | 6. $\int (ax + b)^n dx = \frac{(ax+b)^{n+1}}{a(n+1)} + C$ |
| 7. $\int \frac{1}{ax+b} dx = \frac{1}{a} \log ax + b + C$ | 8. $\int a^{px+q} dx = \frac{1}{p} \frac{a^{px+q}}{\log a} + C$ |
| 9. $\int e^x dx = e^x + C$ | 10. $\int e^{ax} dx = \frac{e^{ax}}{a}$ |
| 11. $\int \sin x dx = -\cos x + C$ | 12. $\int \cos x dx = \sin x + C$ |
| 13. $\int \tan x dx = \log \sec x + C = -\log \cos x + C$ | |
| 14. $\int \cot x dx = \log \sin x + C = -\log \operatorname{cosec} x + C$ | |
| 15. $\int \sec x dx = \log(\sec x + \tan x) + C$ | 16. $\int \operatorname{cosec} x dx = \log(\operatorname{cosec} x - \cot x) + C$ |
| 17. $\int \sec^2 x dx = \tan x + C$ | 18. $\int \operatorname{cosec}^2 x dx = -\cot x + C$ |
| 19. $\int \sec x \tan x dx = \sec x + C$ | 20. $\int \operatorname{cosec} x \cot x dx = -\operatorname{cosec} x + C$ |

Indefinite Integrals Of Some Particular

$$1. \int \frac{dx}{\sqrt{1-x^2}} = \sin^{-1}x + C = -\cos^{-1}x + C$$

$$2. \int \frac{dx}{1+x^2} = \tan^{-1}x + C = -\cot^{-1}x + C$$

$$3. \int \frac{dx}{x\sqrt{x^2-1}} = \sec^{-1}x + C = -\operatorname{cosec} x^{-1} + C$$

$$4. \int \frac{dx}{x^2-a^2} = \frac{1}{2a} \log \left| \frac{x-a}{x+a} \right| + C$$

$$5. \int \frac{dx}{a^2-x^2} = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C$$

$$6. \int \frac{dx}{x^2+a^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$7. \int \frac{dx}{\sqrt{x^2-a^2}} = \log|x + \sqrt{x^2-a^2}| + C$$

$$8. \int \frac{dx}{\sqrt{a^2-x^2}} = \sin^{-1} \frac{x}{a} + C$$

$$9. \int \frac{dx}{\sqrt{x^2+a^2}} = \log|x + \sqrt{x^2+a^2}| + C$$

$$10. \int \sqrt{x^2+a^2} dx = \frac{1}{2}x\sqrt{x^2+a^2} + \frac{a^2}{2} \log|x + \sqrt{x^2+a^2}| + C$$

$$11. \int \sqrt{a^2-x^2} dx = \frac{1}{2}x\sqrt{a^2-x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} + C$$

$$12. \int e^{ax} \sin bx dx = \frac{e^{ax}}{a^2+b^2} [a \sin bx - b \cos bx]$$

$$13. \int e^{ax} \cos bx dx = \frac{e^{ax}}{a^2+b^2} [a \cos bx + b \sin bx]$$

Definite Integrals Of Some Particular

The notation for an indefinite integral is:

$$\int_a^b f(x) dx = [F(x)]_a^b = F(b) - F(a)$$

1. $\int_a^a f(x) dx = 0$

2. $\int_a^b f(x) dx = \int_a^b f(t) dt$

3. $\int_a^b f(x) dx = -\int_b^a f(x) dx$

4. $\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$

5. $\int_a^b f(x) dx = \int_a^b f(a + b - x) dx$

➤ $\int_0^a f(x) dx = \int_0^a f(a - x) dx$

6. $\int_0^{2a} f(x) dx = \int_0^a f(x) dx + \int_0^a f(2a - x) dx$

➤ $\int_0^{2a} f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{if } f(2a - x) = f(x) \\ 0 & , \text{if } f(2a - x) = -f(x) \end{cases}$

7. $\int_{-a}^a f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{if } f(-x) = f(x) \text{ i. e. } f \text{ is an even function} \\ 0 & , \text{if } f(-x) = -f(x) \text{ i. e. } f \text{ is an odd function} \end{cases}$



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HOW LEARNING HAPPENS HERE

- ✓ **CONCEPT CLARITY** FIRST
- ✓ **REGULAR TESTS + FEEDBACK**
- ✓ **DOUBT CLEARING** SESSIONS
- ✓ **PERSONAL ATTENTION** TO EVERY STUDENT
- ✓ **NO ROTE** LEARNING METHODS

RESULTS ARE A BY-PRODUCT OF THE PROCESS

IS THIS COACHING CENTRE RIGHT FOR YOUR CHILD?

DOES YOUR CHILD

- ✓ **STRUGGLE** WITH CONCEPT?
- ✓ **NEED PERSONAL ATTENTION?**
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- ✓ **WANT STRONG FUNDAMENTALS?**
- ✓ **HATE ROTE** LEARNING?

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